Programmation Fonctionnelle Avancée http://www-lipn.univ-paris13.fr/~saiu/teaching/PFA-2010

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2010-12-08



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- Complex library support at run time
 - How do we represent objects in memory?
 - Think about memory words, bits and pointers
 - How do we release memory?
 - The runtime must be written in a low-level language (C, assembly)



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- We don't need to copy anything! We're just building a very small structure (one cons) which refers the given one
 - We should always pass and return pointers to data structures in memory
 - Fast and simple!
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Binary words



Figure: A 32-bit word

- Modern machines have 32- or 64-bit words. There are assembly instructions working efficiently on word-sized data (arithmetics, load, store)
- At the hardware level, memory is untyped: a binary word can represent an integer, a boolean, a float, some characters, a pointer¹, a sum type element with no parameters...

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Boxed vs. unboxed

- boxed: allocate the object in memory, and pass around a pointer to it
- unboxed: pass around the object itself, which is small (word-sized)



```
int f(int x){
   struct big_strict s;
   s.q = x;
   s.w = g(x, &s);
   ...
   return 42;
}
```

- s is visible to g. s remains alive in memory until f returns, so also the functions called by g might access it.
- When f returns s is automatically destroyed: its memory will be reused
- LIFO policy implemented with a stack: push at function entry, pop at function exit
 - Very, very efficient. But not expressive enough.

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Heap allocation and de-allocation

Any reasonable programming language also lets you explicitly create new objects in memory without following a LIFO policy:



A heap with free list

A *heap* is the data structure on which malloc and free are implemented:

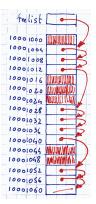


Figure: A 16-word heap with a *free list*: each *unused* word in the *heap* points to the next one. Red words belong to alive objects.

- $10011000100110101010001000_2 = 10001032_{10}$
- Number, memory address, or what else?
- In general we can't tell
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We can reserve a word for runtime type information at the beginning of each object:

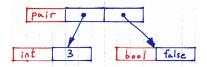


Figure: The pair (3, false) represented with object headers. The words shown in red contain some binary encoding of the type.



Another example with object headers:

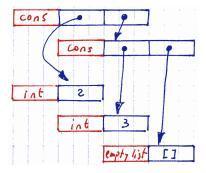


Figure: The list 2 :: 3 :: [], also written as [2; 3], with object headers

Pros

- Easy to understand and implement
- One word per object suffices to encode any type
 - The header can also be a pointer, if needed

Cons



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Object headers - III

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Cons

• Inefficient: we have to unbox everything



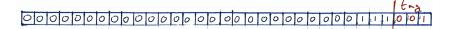
Instead of using a prefix word, we can reserve some bits in a fixed position within a datum to encode its type. Example (3-bit tag):

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000: unique values (booleans, empty list, unit, ...)
001: integer
010: cons
011: character
100: float
101: ref
110: string
111: (not used)
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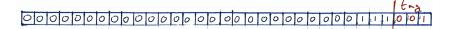
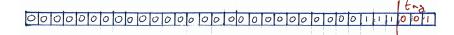


Figure: A 32-bit word with a 3-bit tag. What's this?

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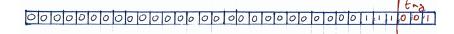
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Figure: A 32-bit word with a 3-bit tag. What's this? The integer 7₁₀



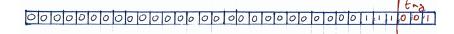
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 - compact: no additional space is used
- Cons:
 - operating on data is harder and possibly slower (think of adding two tagged integers)
 - ...but we can choose tags in a smart way (any ideas?)
 - less space available for the datum payload
 - very few tags available: at most 2^n with n tag bits





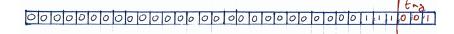
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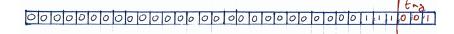
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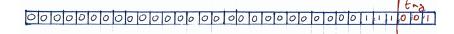
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Tagging within a datum word - Example

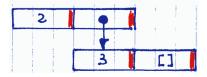


Figure: A list with in-word tags

Notice that we have tagged a pointer. Why can we do it?

- If heap objects are aligned on word boundary, the rightmost two (for 32-bit architectures) or three (for 64-bit architectures) bits are always zero in native pointers.
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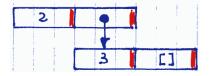


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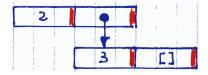


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Alignment: look at the heap again

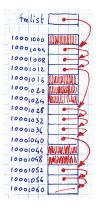


Figure: Think of the binary representation of pointers to heap objects: here any pointer will end with 00 (because addresses in radix 10 are divisible by 4).



In-word tags are more efficient than headers, but we would need much more than two or three bits... We can find a compromise

Use a short in-word tag of two or three bits for the most common types which we want to keep unboxed or boxed without header, reserving one value for boxed objects with headers.

Example (with two-bit in-word tag):

- 00 int (unboxed)
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Hybrid tagging – example

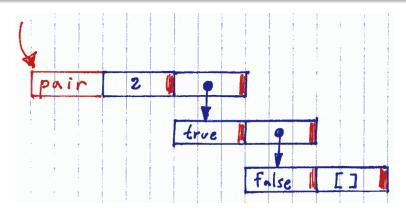


Figure: The pair (2, [true; false]), following the convention of the previous slide. The pair has a header because we didn't consider it "common" enough: but integers, conses and unique values (booleans and the empty list) need no header.

Static typing and tagging

We ignored static typing until now. Does OCaml need runtime tags?

Possible bonus if you answer this in a smart way



We want to work under the illusion that memory is infinite.

- The program just allocates objects, ignoring the problem
- Unneeded objects are automatically destroyed by the runtime, which "wakes up" when needed

Pros:

- No dangling pointers
- No double free
- No (trivial) memory leaks

- Inefficient.
 - Mmm. Is it really inefficient?





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Automatic memory management — Definitions

At a given time, we call heap objects which will never be used again by the program *semantic garbage*.

- The runtime system works with roots (processor registers and stack, global variables): heap objects can only be reached via pointers from roots, or...
- ...from other heap objects. For example, many conses *refer* other conses
- A piece of syntactic garbage is a heap object which can't be reached by recursively following pointers starting from roots
 - Automatic memory management recycles syntactic garbage
 - Because of deep theoretical reasons it's impossible to find all semantic garbage; but recycling syntactic garbage is a conservative approximation

- Tracing garbage collection (or just garbage collection):
 - when the memory is full visit the graph of alive objects, starting from roots;
 - what we didn't visit is garbage: destroy it
- Reference counting
 - count the pointers to each object
 - when an object has zero pointers destroy it
- Only two main approaches. But there are many, many, many variants





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History

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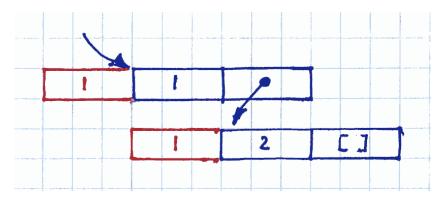
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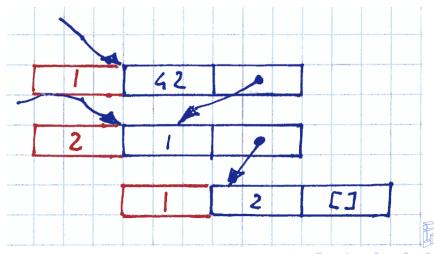
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- George E. Collins responded in 1960 by proposing reference counting as a "more efficient" alternative
- Popularly considered inefficient. Many languages have always been depending on it, but accepted into the mainstream only in the 1990s

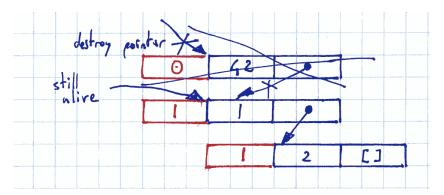
Reference-counting - I



Reference-counting - II



Reference-counting - III



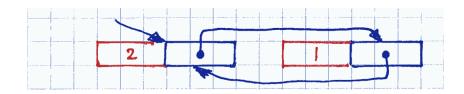


Reference-counting problems - I

- Very inefficient (one word overhead per object, keeping counters up-to-date costs more than payload operations)...
- ...but this is not the main problem



Reference-counting problems - II







Reference-counting problems - III

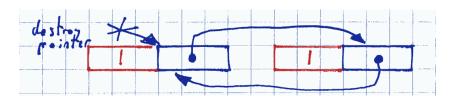


Figure: Circular garbage is never destroyed!



Reference-counting problems - IV

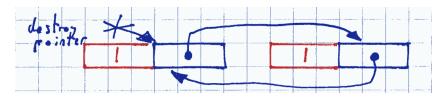


Figure: This is definitely syntactic garbage; but *cyclic* objects can't be destroyed by the reference counter.



Tracing garbage collection

